

SOLUTIONS

1. (c) HCF of 1152 and 1664 = 128
2. (b) $x^2 - 3x - m(m+3) = 0$
 $x^2 + mx - (m+3)x - m(m+3) = 0$
 $\Rightarrow x(x+m) - (m+3)(x+m) = 0$
 $\Rightarrow (x+m)[x - (m+3)] = 0$
 $x+m = 0$ or $x - (m+3) = 0$
 $\Rightarrow x = -m$ or $x = m+3$
3. (c) The given polynomial is $f(x) = (x-2)^2 + 4$ for zeroes,
 $f(x) = 0$
 $\Rightarrow (x-2)^2 + 4 = 0$
 $\Rightarrow (x-2)^2 = -4$

Which is not possible,

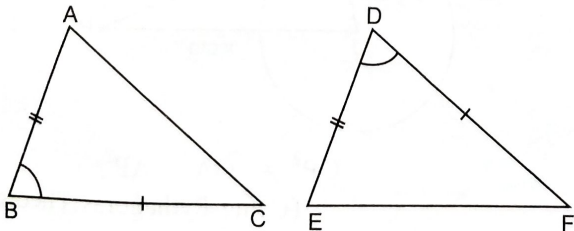
Hence this polynomial has no zeroes.

4. (a) The given equations are $2x - 3y = 1$ and $3x - 2y = 4$
- Here $\frac{a_1}{a_2} = \frac{2}{3}, \frac{b_1}{b_2} = \frac{-3}{-2} = \frac{3}{2}$
 $\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$

The given pair of linear equations has unique solution.

5. (c) Let coordinates of vertices be A(4, 0), B(-1, -1) and C(3, 5)
- $$AB = \sqrt{(-1-4)^2 + (-1-0)^2} = \sqrt{26}$$
- $$BC = \sqrt{(3+1)^2 + (5+1)^2} = \sqrt{52}$$
- $$AC = \sqrt{(3-4)^2 + (5-0)^2} = \sqrt{26}$$
- Since, $AB^2 + AC^2 = BC^2$
 and $AB = AC$
 Hence, triangle is an isosceles right-angled triangle.

6. (c) In $\triangle ABC$ and $\triangle DEF$ $\frac{AB}{DE} = \frac{BC}{DF}$



Also $\triangle ABC \sim \triangle EDF$

This is only possible when $\angle B = \angle D$.

7. (c) Given, $\tan \theta + \cot \theta = 2$

Let $\tan \theta = x$

$$\therefore x + \frac{1}{x} = 2 \Rightarrow x^2 - 2x + 1 = 0$$

On solving the quadratic equation,

$$x = 1 \Rightarrow \tan \theta = 1$$

$$\therefore \theta = 45^\circ$$

\therefore The value of $\sin^3 \theta + \cos^3 \theta$

$$= (\sin 45^\circ)^3 + (\cos 45^\circ)^3$$

$$= \frac{1}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} = \frac{1}{\sqrt{2}}$$

8. (d) Let the y -axis divides in $k : 1$.

Now, according to the question,

$$x = \frac{k \times (5) + 1 \times (-3)}{(k+1)}$$

$$\Rightarrow 0 = \frac{5k-3}{(k+1)} \Rightarrow 5k-3=0$$

$$\Rightarrow k = \frac{3}{5} = 3 : 5$$

9. (d) $\therefore DE \parallel BC$

$\therefore \angle ABC = 70^\circ$ (Corresponding angles)

Using angle sum property of triangle in $\triangle ABC$,

$$\angle ABC + \angle BCA + \angle BAC = 180^\circ$$

$$\Rightarrow \angle BCA = 180^\circ - 70^\circ - 50^\circ = 60^\circ.$$

10. (a) $DE \parallel BC$, if $\frac{AD}{DB} = \frac{AE}{EC}$

$$\Rightarrow \frac{1.28}{2.56} = \frac{0.64}{EC}$$

$$\Rightarrow EC = 1.28 \text{ cm.}$$

11. (c) Infinitely many.

12. (a) Let radius of the circle be r units

Circumference of the circle = $2\pi r$,

Area of the circle = πr^2

A.T.Q

Circumference of the circle = Area of the circle

$$\Rightarrow 2\pi r = \pi r^2$$

$$\Rightarrow r = 2 \text{ units.}$$

13. (b) Let radius of sphere be a cm
 \therefore Surface area of sphere = $4\pi a^2$
 $\therefore 4 \times \pi a^2 = 616$
 $\therefore 4 \times \frac{22}{7} \times a^2 = 616$
 $\Rightarrow a^2 = \frac{616 \times 7}{22 \times 4} = 49$
 $\Rightarrow a = 7$ cm

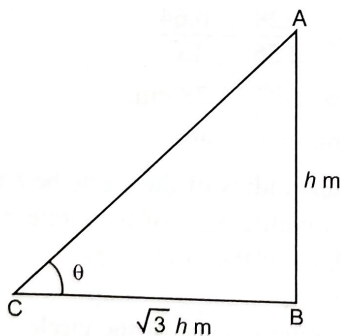
14. (c) \therefore Mean = assumed mean + $\frac{\sum f_i d_i}{\sum f_i}$
 $\therefore x =$ assumed mean.

15. (c) Circumference of smaller wheel = 30π cm
 Circumference of bigger wheel = 50π cm
 Now, $15 \times 50\pi =$ number of revolutions $\times 30\pi$
 \Rightarrow number of revolutions = 25

16. (c) Sum of 100 observations = $100 \times 49 = 4900$
 Correct sum = $4900 - [40 + 20 + 50] + [60 + 70 + 80] = 5000$
 \therefore Correct mean = $\frac{5000}{100} = 50$.

17. (c) Number of lottery tickets = 2000
 Total number of prizes = 16
 \therefore Probability that Abhinav wins a prize
 $= \frac{16}{2000} = \frac{1}{125} = 0.008$

18. (b) Here AB is tower of height h m.
 Its shadow BC = $\sqrt{3}h$ m
 Let θ be the angle of elevation



\therefore In ΔABC , $\tan \theta = \frac{AB}{BC} = \frac{h}{\sqrt{3}h} = \frac{1}{\sqrt{3}}$
 $\tan \theta = \tan 30^\circ$
 $\Rightarrow \theta = 30^\circ$

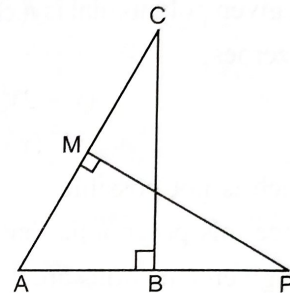
19. (d) Assertion (A) is false but Reason (R) is true.
 20. (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

21. Let the cost of 1 book be ₹ x and the cost of 1 pen be ₹ y .
 According to question,

$$5x + 7y = 79 \quad \dots (i)$$

and $7x + 5y = 77 \quad \dots (ii)$

22. **Given:** In ΔABC , $\angle B = 90^\circ$ and in ΔAMP , $\angle M = 90^\circ$



To prove: (i) $\Delta ABC \sim \Delta AMP$ and

$$(ii) \frac{CA}{PA} = \frac{BC}{MP}$$

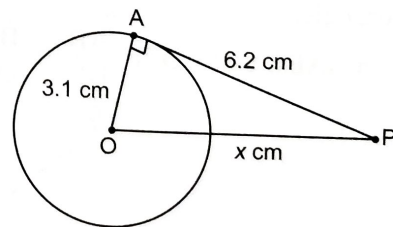
Proof:

(i) In ΔABC and ΔAMP ,
 $\angle ABC = \angle AMP$ (Each 90°)
 $\angle BAC = \angle MAP$ (Common)
 $\therefore \Delta ABC \sim \Delta AMP$ (AA similarity)

(ii) As $\Delta ABC \sim \Delta AMP$,
 $\therefore \frac{AC}{AP} = \frac{BC}{MP}$
 (Ratios of the corresponding sides of similar triangles)

$$\Rightarrow \frac{CA}{PA} = \frac{BC}{MP} \quad \text{Hence proved.}$$

23. In right-angled ΔOAP ,



$$OP^2 = OA^2 + AP^2$$

(Using Pythagoras Theorem)

$$\Rightarrow x^2 = (3.1)^2 + (6.2)^2$$

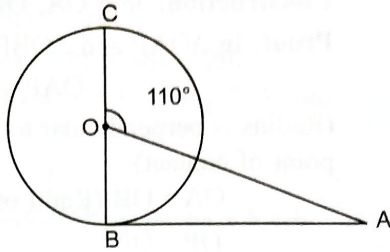
$$\Rightarrow x^2 = 9.61 + 38.44$$

$$\Rightarrow x^2 = 48.05$$

$$\Rightarrow x = 6.93 \text{ cm}$$

OR

Given:



$$\begin{aligned} \therefore \angle AOB + \angle AOC &= 180^\circ \text{ (linear pair)} \\ \therefore \angle AOB &= 180^\circ - \angle AOC \\ &= 180^\circ - 110^\circ = 70^\circ \end{aligned}$$

$$\begin{aligned} \text{In } \triangle AOB, \angle OBA + \angle OAB + \angle AOB &= 180^\circ \\ \therefore 90^\circ + \angle OAB + 70^\circ &= 180^\circ \\ \angle OAB &= 180^\circ - 160^\circ = 20^\circ \end{aligned}$$

24. Circumference of the circle = 44 cm

$$\begin{aligned} \Rightarrow 2\pi r &= 44 \text{ cm} \\ \Rightarrow r &= \frac{44 \times 7}{2 \times 22} = 7 \text{ cm} \\ \therefore \text{Area of the quadrant of a circle} \\ &= \frac{1}{4}\pi r^2 = \frac{1}{4} \times \frac{22}{7} \times 7 \times 7 = \frac{77}{2} \text{ cm}^2 \end{aligned}$$

25. Given, $\tan \theta = \frac{1}{\sqrt{3}}$

$$\text{As we know that } \tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \theta = 30^\circ$$

Putting $\theta = 30^\circ$ in $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta}$, we get

$$\begin{aligned} \frac{\operatorname{cosec}^2 30^\circ - \sec^2 30^\circ}{\operatorname{cosec}^2 30^\circ + \sec^2 30^\circ} &= \frac{(2)^2 - \left(\frac{2}{\sqrt{3}}\right)^2}{(2)^2 + \left(\frac{2}{\sqrt{3}}\right)^2} \\ &= \frac{4 - \frac{4}{3}}{4 + \frac{4}{3}} = \frac{8}{16} = \frac{1}{2} \end{aligned}$$

OR

$$\sin(A - B) = \frac{1}{2} = \sin 30^\circ$$

$$\Rightarrow A - B = 30^\circ \quad \dots(i)$$

$$\cos(A + B) = \frac{1}{2} = \cos 60^\circ$$

$$\Rightarrow A + B = 60^\circ \quad \dots(ii)$$

Adding (i) and (ii), we get

$$2A = 90^\circ \Rightarrow A = 45^\circ$$

Putting the value of in (i), we get

$$45^\circ - B = 30^\circ \Rightarrow B = 15^\circ$$

26. Let $\sqrt{5}$ is a rational number and $\sqrt{5} = \frac{a}{b}$, where a and b are coprime and $b \neq 0$,

$$\begin{aligned} \text{Now, } (\sqrt{5})^2 &= \left(\frac{a}{b}\right)^2 \\ \Rightarrow 5b^2 &= a^2 \quad \dots(i) \end{aligned}$$

$$\Rightarrow 5 \text{ is a factor of } a^2$$

$\therefore a$ is also divisible by 5.

Let $a = 5c$, where c is some integer.

Substituting $a = 5c$ in (i), we get

$$\begin{aligned} 5b^2 &= (5c)^2 \\ \Rightarrow 5b^2 &= 25c^2 \Rightarrow b^2 = 5c^2 \end{aligned}$$

$$\Rightarrow 5 \text{ is a factor of } b^2$$

$\therefore 5$ is a factor of b .

$\therefore 5$ is a common factor of a and b

This contradicts the fact that a and b are coprime so, our assumption is wrong.

Hence, $\sqrt{5}$ is irrational.

27. Let the integer be x and its reciprocal be $\frac{1}{x}$.

According to question,

$$\begin{aligned} x - \frac{1}{x} &= \frac{143}{12} \\ \Rightarrow \frac{x^2 - 1}{x} &= \frac{143}{12} \end{aligned}$$

$$\Rightarrow 12x^2 - 12 = 143x$$

$$\Rightarrow 12x^2 - 143x - 12 = 0$$

$$\Rightarrow 12x^2 - 144x + x - 12 = 0$$

$$\Rightarrow 12x(x - 12) + 1(x - 12) = 0$$

$$\Rightarrow (x - 12)(12x + 1) = 0$$

$$\Rightarrow x = 12 \text{ or } x = -\frac{1}{12}$$

Rejecting $x = -\frac{1}{12}$, because x is an integer.

$$\therefore x = 12$$

\therefore The required integer is 12.

OR

If the equation $x^2 + kx + 64 = 0$ has real roots, then $D \geq 0$.

$$\Rightarrow k^2 - 4 \times 1 \times 64 \geq 0$$

$$\Rightarrow k^2 \geq 256 \Rightarrow k^2 \geq (16)^2$$

$$\Rightarrow k \geq 16 \quad [\because k > 0] \dots(i)$$

If the equation $x^2 - 8x + k = 0$ has real roots, then $D \geq 0$

$$\Rightarrow 64 - 4k \geq 0 \Rightarrow 4k \leq 64$$

$$\Rightarrow k \leq 16 \quad \dots(ii)$$

From (i) and (ii), we get

$$k = 16.$$

28. Let $p(x) = 4x^2 + 4x + 1$

$\therefore \alpha, \beta$ are zeroes of $p(x)$

$$\therefore \alpha + \beta = \text{sum of zeroes} = \frac{-b}{a}$$

$$\Rightarrow \alpha + \beta = \frac{-4}{4} = -1 \quad \dots(i)$$

Also $\alpha \cdot \beta = \text{Product of zeroes} = \frac{c}{a}$

$$\Rightarrow \alpha \cdot \beta = \frac{1}{4} \quad \dots(ii)$$

Now a quadratic polynomial whose zeroes are 2α and 2β .

$$\begin{aligned} x^2 - (\text{sum of zeroes})x + \text{Product of zeroes} \\ &= x^2 - (2\alpha + 2\beta)x + 2\alpha \times 2\beta \\ &= x^2 - 2(\alpha + \beta)x + 4\alpha\beta \\ &= x^2 - 2 \times (-1)x + 4 \times \frac{1}{4} \\ &\quad \text{[Using eq.(i) and (ii)]} \\ &= x^2 + 2x + 1 \end{aligned}$$

29. $\tan(A + B) = \sqrt{3}$

$$\Rightarrow \tan(A + B) = \tan 60^\circ$$

$$\Rightarrow A + B = 60^\circ \quad \dots(i)$$

$$\tan(A - B) = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \tan(A - B) = \tan 30^\circ$$

$$\Rightarrow A - B = 30^\circ \quad \dots(ii)$$

Adding (i) and (ii), we get

$$2A = 90^\circ$$

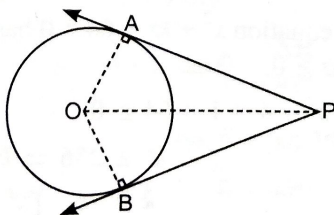
$$\Rightarrow A = \frac{90^\circ}{2} = 45^\circ$$

From (i), $45^\circ + B = 60^\circ$

$$\Rightarrow B = 60^\circ - 45^\circ = 15^\circ$$

Hence, $\angle A = 45^\circ, \angle B = 15^\circ$

30. **Given:** A circle $C(O, r)$. P is a point outside the circle and PA and PB are tangents to a circle.



To prove: $PA = PB$

Construction: Join OA, OB and OP.

Proof: In $\triangle OAP$ and $\triangle OBP$,

$$\angle OAP = \angle OBP = 90^\circ$$

(Radius is perpendicular to the tangent at the point of contact)

$$OA = OB \text{ (Radii of the same circle)}$$

$$OP = OP \text{ (Common)}$$

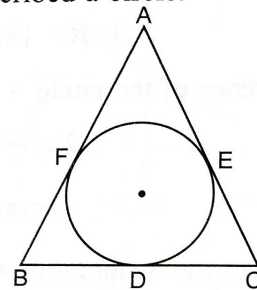
$$\therefore \triangle OAP \cong \triangle OBP \text{ (RHS congruence rule)}$$

$$\Rightarrow PA = PB \text{ (CPCT)}$$

Hence proved.

OR

Given: In an isosceles $\triangle ABC$, $AB = AC$, circumscribed a circle.



To prove: $BD = DC$

Proof: Here, $AB = AC$ (Given)...(i)

$$AF = AE$$

(Tangents from an external point A to a circle are equal) ... (ii)

Subtracting (ii) from (i), we get

$$AB - AF = AC - AE$$

$$\Rightarrow BF = CE \quad \dots(iii)$$

Now, $BF = BD$

(Tangents from an external point B to a circle are equal)

Also, $CE = CD$

(Tangents from an external point C to a circle are equal)

$$\Rightarrow BD = CD$$

\therefore BC is bisected at the point of contact.

Hence proved.

31. Total number of coins = $100 + 50 + 20 + 10 = 180$

(i) Number of 50p coins = 100

$$\therefore \text{Probability of getting a 50p coin}$$

$$= \frac{100}{180} = \frac{5}{9}$$

(ii) Number of ₹ 5 coins = 10

$$\text{Number of coins other than ₹ 5 coins}$$

$$= 180 - 10 = 170$$

$$\begin{aligned} \therefore \text{Probability of not getting a ₹ 5 coin} \\ = \frac{170}{180} = \frac{17}{18} \end{aligned}$$

(iii) Number of ₹2 coins = 20

$$\begin{aligned} \therefore \text{Probability of getting ₹ 2 coin} \\ = \frac{20}{180} = \frac{1}{9} \end{aligned}$$

32. Let the speed of the train be x km/h

Distance travelled = 360 km

$$\therefore \text{Time taken} = \frac{360}{x} \text{ hours}$$

The speed of the train becomes $(x + 5)$ km/h, if the speed had been 5 km/h more.

Distance = 360 km

$$\therefore \text{Time taken} = \frac{360}{x+5} \text{ hours}$$

$$\text{According to question, } \frac{360}{x} = \frac{360}{x+5} + 1$$

$$\Rightarrow \frac{360}{x} - \frac{360}{x+5} = 1$$

$$\Rightarrow \frac{360(x+5) - 360x}{x(x+5)} = 1$$

$$\Rightarrow 1800 = x^2 + 5x$$

$$\Rightarrow x^2 + 5x - 1800 = 0$$

$$\Rightarrow x^2 + 45x - 40x - 1800 = 0$$

$$\Rightarrow (x + 45)(x - 40) = 0$$

$$\Rightarrow x = -45 \text{ or } x = 40$$

Rejecting $x = -45$,

\therefore Speed of the train = 40 km/h

OR

Let the two numbers be x and $x - 5$.

According to question,

$$\frac{1}{x-5} - \frac{1}{x} = \frac{1}{10} \quad \left(\text{Since } \frac{1}{x-5} > \frac{1}{x} \right)$$

$$\Rightarrow \frac{x - x + 5}{(x-5)x} = \frac{1}{10}$$

$$\Rightarrow (x-5)x = 50$$

$$\Rightarrow x^2 - 5x - 50 = 0$$

$$\Rightarrow (x-10)(x+5) = 0$$

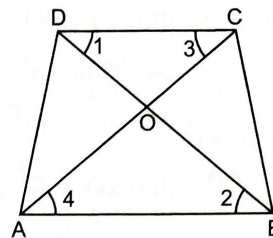
$$\Rightarrow x = 10 \text{ or } x = -5$$

When $x = 10$, then $x - 5 = 10 - 5 = 5$

When $x = -5$, then $x - 5 = -5 - 5 = -10$

Thus, the required numbers are either 10 and 5 or -5 and -10 .

33. Given: Diagonals AC and BD intersect at O.



$AB \parallel DC$

$$\text{To Prove: } \frac{OA}{OC} = \frac{OB}{OD}$$

Proof: In $\triangle AOB$ and $\triangle COD$

$$\angle 1 = \angle 2$$

$$\angle 3 = \angle 4 \quad [\text{Alternate angles}]$$

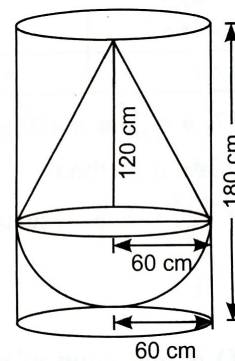
$$\therefore \triangle AOB \sim \triangle COD \quad [\text{Alternate angles}]$$

$$\Rightarrow \frac{OA}{OC} = \frac{OB}{OD}$$

[Corresponding sides of similar triangles]

34. Radius of cone = 60 cm

Height of cone = 120 cm



$$\therefore \text{Volume of cone} = \frac{1}{3} \pi r^2 h$$

$$= \frac{1}{3} \pi \times (60)^2 \times 120$$

$$= 144000\pi \text{ cm}^3$$

Radius of hemisphere = 60 cm

$$\therefore \text{Volume of hemisphere} = \frac{2}{3} \pi r^3 = \frac{2}{3} \pi \times (60)^3$$

$$= 144000\pi \text{ cm}^3$$

\therefore Volume of solid = Volume of cone + Volume of hemisphere

$$= 144000\pi \text{ cm}^3 + 144000\pi \text{ cm}^3$$

$$= 288000\pi \text{ cm}^3$$

Now, Volume of cylinder = $\pi r^2 h$

$$= \pi \times (60)^2 \times 180 = 648000\pi \text{ cm}^3$$

Volume of water left in the cylinder = Volume of cylinder - Volume of solid

$$\begin{aligned}
 &= 648000\pi \text{ cm}^3 - 288000\pi \text{ cm}^3 \\
 &= 360000\pi \text{ cm}^3 \\
 &= 360000 \times \frac{22}{7} \text{ cm}^3 \\
 &= 1131428.57 \text{ cm}^3 \\
 &= \frac{1131428.57}{1000} \text{ l} = 1131.42 \text{ l}
 \end{aligned}$$

OR

₹ 24 is the cost for fencing 1 m of circular field.

35. Let $A = 57$, $h = 3$

Number of mineral water bottles	Number of boxes (f_i)	Class marks (x_i)	$u_i = \frac{x_i - A}{h}$	$f_i u_i$
49.5 - 52.5	20	51	-2	-40
52.5 - 55.5	120	54	-1	-120
55.5 - 58.5	105	57 = A	0	0
58.5 - 61.5	125	60	1	125
61.5 - 64.5	30	63	2	60
Total	$n = 400$			$\Sigma f_i u_i = 25$

Here $A = 57$, $h = 3$, $n = 400$ and $\Sigma f_i u_i = 25$

By step-deviation method,

$$\begin{aligned}
 \text{Mean, } \bar{x} &= A + h \times \frac{1}{n} \times \Sigma f_i u_i = 57 + 3 \times \frac{1}{400} \times 25 \\
 &= 57 + \frac{75}{400} = 57 + 0.1875 = 57.1875 \approx 57.19 \text{ (approx.)}
 \end{aligned}$$

36. (i) Here O is mid point of AC and BD.

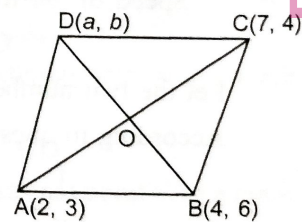
By mid-point formula,

$$\therefore \frac{2+7}{2} = \frac{a+4}{2}$$

$$\Rightarrow 9 = a + 4 \Rightarrow a = 5$$

and $\frac{3+4}{2} = \frac{6+b}{2}$

$$\Rightarrow 7 = 6 + b \Rightarrow b = 1$$



(ii), As we know that diagonals of a parallelogram bisect each other.

Let fourth vertex of the parallelogram be (x, y) .

By mid-point formula,

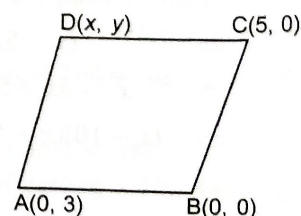
Now, $\frac{0+x}{2} = \frac{0+5}{2}$

$$\Rightarrow x = 5$$

and $\frac{0+y}{2} = \frac{3+0}{2}$

$$\Rightarrow y = 3$$

\therefore Fourth vertex is $(5, 3)$



₹ 5280 is the cost for fencing = $\frac{1}{24} \times 5280$
= 220 m of circular field.

Circumference of the field = 220 m

$$\Rightarrow 2\pi r = 220$$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 220$$

$$\Rightarrow r = \frac{220 \times 7}{44} = 35 \text{ m}$$

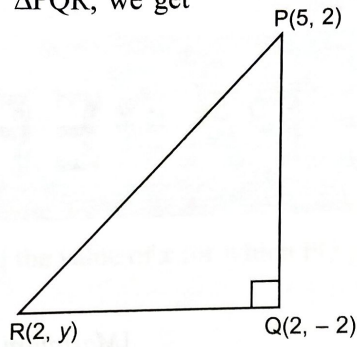
\therefore Area of the field = $\pi r^2 = \pi(35)^2 = 1225\pi \text{ m}^2$

Cost of ploughing = ₹ 0.50 per m^2

Total cost of ploughing the field

$$= ₹ 1225\pi \times 0.50 = ₹ 1925$$

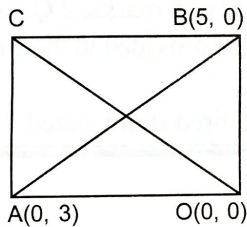
(iii), Using Pythagoras theorem in right-angled ΔPQR , we get



$$\begin{aligned} (PR)^2 &= (PQ)^2 + (QR)^2 \\ \Rightarrow (5-2)^2 + (2-y)^2 &= (5-2)^2 + (2+2)^2 \\ &\quad + (2-2)^2 + (y+2)^2 \\ \Rightarrow 9 + 4 + y^2 - 4y &= 9 + 16 + y^2 + 4y + 4 \\ \Rightarrow -4y &= 16 + 4y \Rightarrow y = -2 \end{aligned}$$

OR

As we know that diagonals of rectangle are equal.



$$\begin{aligned} \therefore AB &= OC \\ \therefore AB &= \sqrt{(5-0)^2 + (0-3)^2} \\ &= \sqrt{25+9} = \sqrt{34} \end{aligned}$$

Hence $AB = OC = \sqrt{34}$ units

37. (i) Given, $a_6 = 16000$
 $a + 5d = 16000$... (i)

$a_9 = 22600$
 $a + 8d = 22600$... (ii)

From (i) and (ii), we get

$$\begin{aligned} d &= 2200 \\ \therefore a + 5(2200) &= 16000 \\ a &= 16000 - 11000 = 5000 \end{aligned}$$

(ii) $a_n = 29200$
 $\Rightarrow 29200 = a + (n-1)d$
 $\Rightarrow 29200 = 5000 + (n-1)2200$
 $\Rightarrow \frac{24200}{2200} = n-1 \Rightarrow n = 12$

In 12th year the production of the company will be 29200.

(iii) $a_7 = a + 6d$
 $a_4 = a + 3d$
 $a_7 - a_4 = a + 6d - a - 3d$
 $= 3d = 3 \times 2200 = 6600$

OR

$$\begin{aligned} a_{12} - a &= a + 11d - a = 11d \\ &= 11 \times 2200 = 24200 \end{aligned}$$

38. (i) Distance AP = Speed \times Time
 $= \frac{720 \times 1000}{3600} \times 15 = 3000$ m

(ii) Distance AP = Speed \times time
 $= \frac{360 \times 1000}{3600} \times 15 = 1500$ m

(iii) Let H be the constant height at which the jet is flying.

In ΔABQ

$$\tan 60^\circ = \frac{AQ}{BQ}$$

$$\Rightarrow BQ = \frac{H}{\sqrt{3}}$$

In ΔPBD $\tan 30^\circ = \frac{PD}{BD}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{H}{BQ + QD}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{H}{\frac{H}{\sqrt{3}} + 3000}$$

(QD = AP)

$$\Rightarrow \left(\frac{H}{\sqrt{3}} + 3000 \right) \frac{1}{\sqrt{3}} = H$$

$$\frac{H}{3} + \frac{3000}{\sqrt{3}} = H$$

$$H = \frac{3 \times 3000}{2\sqrt{3}}$$

$$= 1500\sqrt{3} \text{ m}$$

OR

In $\Delta ABQ = \tan 60^\circ = \frac{AQ}{BQ}$

$$\Rightarrow BQ = \frac{AQ}{\sqrt{3}}$$

Now in $\Delta PBD \tan 30^\circ = \frac{PD}{BD}$

$$\frac{1}{\sqrt{3}} = \frac{AQ}{BQ + QD} \quad (AQ = PD)$$

$$AQ = \frac{BQ + QD}{\sqrt{3}}$$

$$= \frac{AQ}{\sqrt{3} \times \sqrt{3}} + \frac{QD}{\sqrt{3}}$$

$$\Rightarrow \frac{2AQ}{3} = \frac{QD}{\sqrt{3}}$$

$$\Rightarrow AQ = \frac{3 \times 1500}{2 \times \sqrt{3}} = 750\sqrt{3} \text{ m}$$

PK@CW